

Roll No.

Total No. of Pages : 02

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B.Tech. (Mechanical Engg.) (Sem.-2)

**MATHEMATICS-II**

Subject Code : BTAM-203-18

M.Code : 76256

Date of Examination : 08-12-2023

Time : 3 Hrs.

Max. Marks : 60

**INSTRUCTIONS TO CANDIDATES :**

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION - B & C have FOUR questions each.
3. Attempt any FIVE questions from SECTION B & C carrying EIGHT marks each.
4. Select atleast TWO questions from SECTION - B & C.

**SECTION-A**

1. Answer briefly :

a) Define integrating factor. Is it unique for a given differential equation?

b) Give Bernoulli's equation. Explain in brief method to solve it.

c) Solve  $ye^{xy} dx + (xe^{xy} + 2y) dy = 0$ .

d) Solve in series the differential equation  $\frac{d^2y}{dx^2} - y = 0$ .

e) Solve  $\frac{d^2y}{dx^2} + \frac{1}{x} \frac{dy}{dx} = 0$ .

f) Show that an analytic function with constant modulus is constant function.

g) Find the transformation which maps the points  $-1, i, 1$  of the  $z$ -plane onto  $1, i, -1$  of the  $w$ -plane, respectively.

h) State Liouville's theorem.

i) Evaluate  $\int_C \frac{z^2 - 2z + 1}{(z-1)^2} dz$ , where  $C$  is  $|z| = 2$ .

j) Find the Laurent's series expansion of  $f(z) = \frac{z}{(z^2 - 1)(z^2 + 4)}$  in the region  $|z| < 2$ .

### SECTION-B

2. a) Solve  $\tan y \frac{dy}{dx} + \tan x = \cos y \cos^2 x$ .  
b) Solve  $(xy^3 + y)dx + 2\{x^2y^2 + x + y^4\}dy = 0$ .
3. a) Solve  $y - 2px = \tan^{-1}(xp^2)$ .  
b) Solve  $y = 2px + y^2p^3$ .
4. Using the method of variation of parameters, solve  $\frac{d^2y}{dx^2} + 4y = \tan 2x$ .
5. Solve  $x^2 \frac{d^2y}{dx^2} + 4x \frac{dy}{dx} + 2y = e^x$ .

### SECTION-C

6. If  $f(z)$  is a regular function of  $z$ , prove that
$$\left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) |f(z)|^2 = 4|f'(z)|^2$$
7. Find the harmonic conjugate and the analytic function whose imaginary part is  $e^{-x}(x \cos y + y \sin y)$ .
8. State Cauchy Residue theorem. Hence evaluate  $\int_C \frac{z \cos z}{(z - \pi/2)^3} dz$ , where  $C$  is  $|z-1|=1$ .
9. Evaluate:  $\int_0^\infty \frac{\cos ax}{x^2 + 1} dx$ .

**NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.**